Practice C

Evaluate the expression.

1.
$$3^{-4} \cdot 3^{-1}$$

2.
$$9^{-4} \cdot 9^8$$

3.
$$(5^{-1})^4$$

4.
$$\frac{1}{10^{-5}}$$

5.
$$\frac{5^{-6}}{5^{-9}}$$

6.
$$\frac{8^{-10}}{8^{-8}}$$

7.
$$15\left(\frac{3}{5}\right)^{-1}$$

8.
$$32\left(\frac{2^{-4}}{2^3}\right)$$

9.
$$4-2 \cdot \left(\frac{7}{12^0}\right)$$

Simplify the expression. Write your answer using only positive exponents.

10.
$$(4x^{-3}y^4)^{-2}$$

11.
$$\frac{1}{9x^{-4}v^{-8}}$$

12.
$$\frac{1}{6x^4y^{-10}}$$

13.
$$\frac{1}{(4x^{-5})^{-2}}$$

14.
$$\frac{8}{(-2d^2)^{-4}}$$

15.
$$\frac{(2x)^{-4}y^8}{-x^5y^{-3}}$$

16.
$$\frac{x^{-6}y^4}{(-3x^2)^{-4}y^{-1}}$$

$$17. \quad \frac{20x^3y^{-4}}{(2x^{-4}y^{-1})^2}$$

18.
$$\frac{(4x^{-4}y^7)^2}{24x^{-6}y^2}$$

Tell whether the statement is *true* or *false* for all nonzero values of *a* and *b*. If it is *false*, give a counterexample.

19.
$$\frac{a^{-5}}{a^{-6}} = \frac{1}{a}$$

20.
$$\frac{b^{-1}}{a^{-1}} = \frac{a}{b}$$

21.
$$\frac{1}{a^{-1} + b^{-1}} = a + b$$

- **22. Guitar** The world's smallest guitar is only 10^{-6} meter tall. An average guitar is about 10^{0} meter tall. How many times taller is an average guitar than the world's smallest guitar?
- **23**. **Knitting Needles** A size 1 knitting needle has a diameter of about 4^{-1} centimeter and a size 8 knitting needle has a diameter of about 2^{-1} centimeter.
 - **a.** How many times larger is the diameter of a size 8 needle than the diameter of a size 1 needle?
 - **b.** Suppose that each needle is 14 inches long. Write expressions for the approximate volume of each size of knitting needle. Use the formula for the volume of a cylinder $V = \pi r^2 h$.
 - **c.** How many times larger is the approximate volume of a size 8 needle than the approximate volume of a size 1 needle?
 - **d.** Are your approximations in part (b) overestimates or underestimates? *Explain* your reasoning.